

Name: Key
Algebra 1

Date: _____ Period: _____
Day 14 - Adding and Subtracting Polynomials

A polynomial is a monomial or the sum of monomials, each called a term of the polynomial. Some polynomials have special names:

- A binomial is the sum of two monomials.
- A trinomial is the sum of three monomials.

↑ one term

The degree of a monomial is the sum of the exponents of all its variables. A nonzero constant term has degree 0, and zero has no degree.

The degree of a polynomial is the highest degree of any of the terms in the polynomial.

Example $5x - 2x^2 + 1$ has a degree of 2 and is called quadratic

| Degree | Name |
|-----------|--|
| 0 | constant |
| 1 | linear |
| 2 | quadratic |
| 3 | cubic |
| 4 | quartic |
| 5 | quintic |
| 6 or more | 6 th degree, 7 th degree, etc. |

When the terms of a polynomial are arranged so that the terms are in order from least to greatest degree, the polynomial is in Standard form.

Determine whether the following expression is a polynomial. If so, identify the polynomial as a monomial, binomial, or trinomial. Then find the degree of the polynomial. NO: neg/fractional/variable exponent

| Expression | Polynomial? | Monomial, Binomial, or Trinomial? | Degree of the Polynomial? |
|---|------------------------|-----------------------------------|---------------------------|
| $3x - 7xyz$ | Yes | Binomial | 3 |
| -25 | Yes | monomial | 0 |
| $7n^3 + 3n^{-4}$ | NO (negative exponent) | — | — |
| $9x^3 + 4x + x + 4 + 2x$ $9x^3 + 7x + 4$ | Yes | Trinomial | 3 |

NO: variable in denominator

Determine whether each expression is a polynomial. If it is a polynomial, find the degree and determine whether it is a monomial, binomial, or trinomial.

- $7ab + 6b^2 - 2a^3$ Yes, Degree 3, Trinomial
- $2y - 5 + 3y^2$ Yes, degree 2, trinomial
- $3x^2$ Yes, degree 2, monomial
- $\frac{4m}{3p}$ NO - variable in denominator
- $5m^2p^3 + 6$ Yes, Degree 5; Binomial
- $5a^{-4} + 6a$ NO - negative exponent

Write each polynomial in standard form. Identify the leading coefficient. →

7. $2x^5 - 12 + 3x$ $2x^5 + 3x - 12$
LC: 2

8. $-4d^4 + 1 - d^2$ $-4d^4 - d^2 + 1$
LC: -4

9. $4z - 2z^2 - 5z^4$ $-5z^4 - 2z^2 + 4z$
LC: -5

10. $2a + 4a^3 - 5a^2 - 1$
 $4a^3 - 5a^2 + 2a - 1$
LC: 4

Number being multiplied by the term w/ highest degree
(first coefficient when in standard form)

Find each sum or difference.

Combine Like terms - same variables & exponent

11. $(6x^3 - 4) + (-2x^3 + 9)$
 $4x^3 + 5$

12. $(g^3 - 2g^2 + 5g + 6) - (g^2 + 2g)$
Distribute -1
 $g^3 - 2g^2 + 5g + 6 - g^2 - 2g$
 $g^3 - 3g^2 + 3g + 6$

13. $(4 + 2a^2 - 2a) - (3a^2 - 8a + 7)$
 $4 + 2a^2 - 2a - 3a^2 + 8a - 7$
 $-a^2 + 6a - 3$

14. $(8y - 4y^2) + (3y - 9y^2)$
 $-13y^2 + 11y$

15. $(-4z^3 - 2z + 8) - (4z^3 + 3z^2 - 5)$
 $-4z^3 - 2z + 8 - 4z^3 - 3z^2 + 5$
 $-8z^3 - 3z^2 - 2z + 13$

16. $(-3d^2 - 8 + 2d) + (4d - 12 + d^2)$
 $-2d^2 + 6d - 20$

17. $(y + 5) + (2y + 4y^2 - 2)$
 $4y^2 + 3y + 3$

18. $(3n^2 - 5n + n^2) - (-8n^2 + 3n^3)$
 $3n^2 - 5n + n^2 + 8n^2 - 3n^3$
 $-3n^3 + 11n^2 - 5n$

19. The total number of students T who traveled for spring break consists of two groups: students who flew to their destinations F and students who drove to their destination D . The number (in thousands) of students who flew and the total number of students who flew or dove can be modeled by the following equations, where n is the number of years since 1995.

$T = 14n + 21$ $F = 8n + 7$

a. Write the equation that models the number of students who drove their destination for this time period.

$D = 14n + 21 - (8n + 7)$ → $D = 6n + 14$

b. Predict the number of students who will drive to their destination in 2012.

$D = 6(17) + 14$
 $= 102 + 14 = 116 \text{ students}$

$\frac{2012 - 1995}{17} = n$

c. How many students will drive or fly to their destination in 2015?

$T = 14(20) + 21$
 $= 280 + 21$
 $= 301 \text{ students}$

$\frac{2015 - 1995}{20} = n$